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**KINEMATICS AND DYNAMICS STUDY ON THE BEADS OF THE MAIN AXLE
BEARING FOR TECHNOLOGICAL SYSTEMS WITH HIGH ROTATION SPEED**

Daniel Popescu*, Ștefan Buzatu, Roxana-Cristina Popescu

* Autovehicles Department, Faculty of Mechanics, University of Craiova,
Department of Life and Environmental Physics, "HoriaHulubei" National Institute of Physics and
Nuclear Engineering;
Department of Science and Engineering of Oxide Materials and Nanomaterials, Faculty of Applied
Chemistry and Materials Science, Politehnica University of Bucharest;

ABSTRACT

The paper presents a mathematical model for the analysis of kinematics and dynamics of the beads of the main axle bearing inside a high speed cutting machine tool. The use of this model creates the premises of determining the bearings rigidities in order to analyze the stability of the vibration.

KEYWORDS: kinematics, dynamics, bearing bead, high cutting speed, rigidity, stability.

INTRODUCTION

The main characteristics which reflect the level of improvement and exploiting at machine tools are: productive capacity, high stiffness, easy manipulation, etc. Simultaneously, a perfecting in the technological processes was needed, by means of mechanization, automation and intensified operating modes, leading to a rigorous design of the cutting tools.

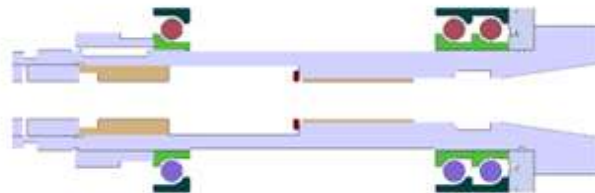
The increased performances of the machine tools, of the CNC machining centers, the continuous development of new products, or products manufactured using CAD/CAM techniques, contribute to the increased precision of the manufactured parts.

Also, the CNC machining centers are evolving by means of:

- Having an increased productivity and flexibility by reducing the non-productive times;
- Developing a surveillance and security system;
- Increasing the dynamic performances (high rigidity, higher cutting speeds, enhanced positioning accuracy);
- Multi-spindle machines for highly complex parts.

In this context, the rigidity of the main spindle of the machine tool has a particular importance for the increase in dimensional precision and the quality of the obtained surfaces (Figure 1).

Figure 1:



Longitudinal section through the main axis;

MATERIALS AND METHODS

The article proposes a method to analyse the kinematics and dynamics of the bearing beads of a high speed rotating shaft, by using the derivative axiom of momentum and the derivative axiom of angular momentum. It creates the premises for the analysis of the axle bearing stiffness.

RESULTS AND DISCUSSION

It was experimentally found that the bearing's rigidities are not constant, these being influenced by the final loading and the axle speed rotation.

For this purpose, it is necessary to make an evaluation of the kinematics and dynamics of the beads from the rolling bearings. Figure 2 presents a bearing bead during the dynamic loading of the spindle.

We consider a reference system Txyz, which is attached to the bead and is chosen as following:

Tx- parallel with the longitudinal axis of the spindle;

Ty- radial axis;

Tz- tangent axis;

We record:

α_i = the contact angle of the bead with the interior ring;

α_e = the contact angle of the bead with the exterior ring.

We consider B the contact point of the bead with the exterior ring. Because the bead performs a rolling movement towards the exterior ring, we accept:

Formulae 1:

$$\vec{v}_B = \vec{v}_T + \vec{\omega}_x \vec{T}_B = (v_{T_x} - \omega_z r \cdot \cos \alpha_e) \vec{i} + (v_{T_y} - \omega_z r \cdot \sin \alpha_e) \vec{j} + (v_{T_z} + \omega_x r \cdot \cos \alpha_e - \omega_y r \cdot \sin \alpha_e) \vec{k} \quad (1)$$

Thus:

Formulae 2:

$$\begin{cases} v_{T_x} - \omega_z r \cdot \cos \alpha_e = 0 \\ v_{T_y} + \omega_z r \cdot \sin \alpha_e = 0 \\ v_{T_z} + \omega_x r \cdot \cos \alpha_e - \omega_y r \cdot \sin \alpha_e = 0 \end{cases} \quad (2)$$

In case of C, which is the contact point of the bead with the interior ring:

Formulae 3:

$$\vec{v}_B = \vec{v}_T + \vec{\omega}_x \vec{OC} = (v_{T_x} + \omega_z r \cdot \cos \alpha_i) \vec{i} + (v_{T_y} - \omega_z r \cdot \sin \alpha_i) \vec{j} + (v_{T_z} - \omega_x r \cdot \cos \alpha_i - \omega_y r \cdot \sin \alpha_i) \vec{k} \quad (3)$$

Supposing that between the interior of the ring and the bead is no gliding, the velocity of the point C must be tangent (parallel with Tz) and equal in size with the velocity of the point C, belonging to the interior ring.

Formulae 4,5:

$$\vec{v}_C = \Omega \cdot R_C \vec{k} \quad (4)$$

R_C = contact radius;

$$\begin{cases} v_{T_x} + \omega_z r \cdot \cos \alpha_i = 0 \\ v_{T_y} - \omega_z r \cdot \sin \alpha_i = 0 \\ v_{T_z} - \omega_x r \cdot \cos \alpha_i + \omega_y r \cdot \sin \alpha_i = \Omega R_C \end{cases} \quad (5)$$

The condition for the first two equations in (2) and (5) to be fulfilled is:

Formulae 6:

$$\begin{cases} v_{Tz} = v_{Ty} = 0; \\ \omega_z = 0; \end{cases} \quad (6)$$

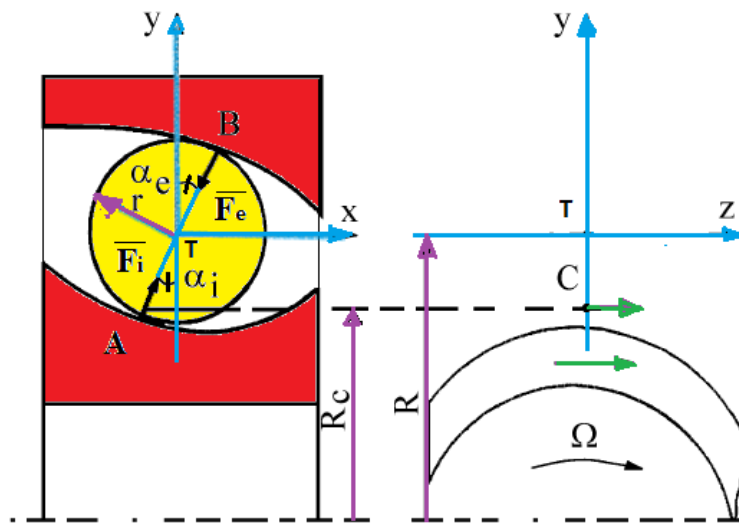
We consider Wb , the angular rotation velocity of the bead center around the axis of the shaft. We can write:

Formulae 7:

$$v_{Tz} = \Omega b \cdot R \quad (7)$$

Where R = the radius of the circle opened by the center of the bead;

Figure 2:



The loading of the bearing bead during the dynamic stress applied to the spindle;

Corresponding to figure 2, we have:

Formulae 8:

$$\begin{aligned} R &= R_C + r \cos \alpha_i \\ R &= R_e - r \cos \alpha_e - d \\ R_C &= R_e - r (\cos \alpha_e + \cos \alpha_i) - d \end{aligned} \quad (8)$$

It is accepted that $\omega_y = 0$. The last relations from (2) and (5) become:

Formulae 9:

$$\begin{aligned} \Omega_b (R_e - r \cos \alpha_e - d) + \omega_x r \cos \alpha_e &= 0 \\ \Omega_b (R_e - r \cos \alpha_e - d) - \omega_x r \cos \alpha_i &= \Omega [R_e - r (\cos \alpha_e + \cos \alpha_i) - d] \end{aligned} \quad (9)$$

Because the variation of α_i and α_e around α is very small, we have:

Formulae 10:

$$\begin{aligned} \omega_x &= \frac{-\Omega [R_e - 2r \cos \alpha - d]}{2r \cos \alpha} = -K_1 \Omega \\ \Omega_b &= \frac{\Omega [R_e - 2r \cos \alpha - d]}{2(R_e - r \cos \alpha - d)} = K_2 \Omega \end{aligned} \quad (10)$$

Having K_1 and K_2 dependent on the construction of the bearing:

Formulae 11:

$$\begin{aligned} K_1 &= \frac{R_e - 2rcos\alpha - d}{2rcos\alpha} \\ K_2 &= \frac{R_e - 2rcos\alpha - d}{2(R_e - rcos\alpha - d)} \end{aligned} \quad (11)$$

The dynamic analysis of the bead is made by using the impulse derivative axioms and the kinetic momentum axiom. These are given by the following relations:

Formulae 12-16:

$$m_b \vec{a}_T = \vec{F}_i + \vec{F}_e \quad (12)$$

$$\vec{a}_T = -\Omega_b^2 R \vec{j} \quad (13)$$

$$\vec{F}_i = F_j \sin\alpha_e \vec{i} + F_i \cos\alpha_i \vec{j} \quad (14)$$

$$\vec{F}_e = -F_e \sin\alpha_e \vec{i} - F_e \cos\alpha_e \vec{j} \quad (15)$$

$$\begin{cases} F_i \sin\alpha_i - F_e \sin\alpha_e = 0 \\ F_i \cos\alpha_i - F_e \cos\alpha_e = -m_b \Omega_b^2 R \end{cases} \quad (16)$$

Where:

\vec{a}_T = the bead weight center acceleration, where the bead makes a rotation movement around the bearing;

\vec{F}_i = the interaction force between the bead and the interior ring;

\vec{F}_e = the interaction force between the bead and the exterior ring;

The kinetic moment axiom:

Formulae 17:

$$m_b \cdot \vec{r}_T \times \vec{a} + \Rightarrow_{J_T} \vec{\varepsilon} + \vec{\omega} \times \left(\Rightarrow_{J_T} \vec{\omega} \right) = \vec{M}_T \quad (17)$$

Thus, we have:

Formulae 18-20:

$$\begin{cases} \vec{r} = \vec{0} \\ (\vec{\varepsilon} = 0) \end{cases} \quad (18)$$

$$\cdot \vec{\omega} \times \left(\Rightarrow_{J_T} \vec{\omega} \right) = \vec{M}_T \quad (19)$$

$$\Rightarrow_{J_T} = \begin{pmatrix} J & 0 & 0 \\ 0 & J & 0 \\ 0 & 0 & J \end{pmatrix} \quad (20)$$

Where:

$\vec{\Rightarrow}_J$ = inertia tensor of the bead relative to its own landmark, with attached matrix;

J = inertia moment of the bead, relative to any diametric axis;

Formulae 21:

$$\vec{\omega} \cdot \vec{\omega} x \left(\vec{\Rightarrow}_J \cdot \vec{\omega} \right) = 0 \quad (21)$$

\vec{M}_T = the resulting moment of \vec{F}_e and \vec{F}_i forces relative to point T;

We have:

Formulae 22:

$$\vec{M}_T = 0 \quad (22)$$

The equation (21) is completely satisfied.

CONCLUSION

- The kinematic and dynamic analysis of the beads of the main axle bearing creates the premises to the analysis of their rigidity;
- In order to assure the equilibrium condition, the constant K_1 and K_2 are highlighted; these depend on the constructive characteristics of the spindles;
- The dynamic analysis of the bead is made by using the impulse derivative axioms and the kinetic moment derivative axiom;
- For the present application, these are completely satisfied.

REFERENCES

- [1] Crolet, A., "Contribution a l'etude de l'influence du comportement vibratoire du system "piece-outil-machine" sur la qualite de surface obtenue en tournage de superfinition", Doctorat de l'Institut National Polytechnique de Lorraine, 2008.
- [2] Ditu, V., "Basics of cutting metals- Theory and applications", Matrix Rom Publisher, 2008, ISBN 978-973-755-444-4.
- [3] Folea, M., Lupulescu, N.B., Lancea, C., "Economical Impact of Using High Speed Machines", Modern technologies, Quality & Restructuring, vol. 1, 2003, pp. 113-116, ISBN 9975-9748-0-5.
- [4] Ispas, C., Simion, F.P., "Vibrations in machine tools. Theory and applications", Romanian Academy Publishing, 1986, pp. 50-82.
- [5] Landers, R.G., "Process Analysis and Control of Machining Operation", Washington University Revue, 2002.
- [6] Popescu, D., Ispas, C., "Grinding process dynamics", SITECH Publishing, Craiova, 1999.
- [7] Popescu, D., "Theoretical and experimental contributions regarding the improvement of the processing precision in interior grinding tools", PhD thesis, Politehnica University of Bucharest, 1999.

AUTHOR BIBLIOGRAPHY

	<p>Daniel Popescu Associate Professor at University of Craiova, Faculty of Mechanics; Competence domains: machine tool design, designing machinery for deformation processing, special machinery, industrial logistics, flexible systems for processing, integrated systems for fabrication.</p>
	<p>Ștefan Buzatu Lecturer at University of Craiova, Faculty of Mechanics; Competence domains: machine precision, measurement and control equipments and methods, inventics, industrial property.</p>
	<p>Roxana-Cristina Popescu Engineer at “HoriaHulubei” National Institute of Physics and Nuclear Engineering, Department of Life and Environmental Science; Master Student at Politehnica University of Bucharest, Faculty of Applied Chemistry and Materials Science; Competence domains: nanomaterials, biomaterials, in vitro and in vivo materials testing, stress analysis, computational stress analysis and modeling.</p>